



Based on the postulates Bohr derived the formulae for
 (i) radius of the stationary orbits
 (ii) the total energy of the electron in the orbit

Coulombic attraction force = Centrifugal force

$$\frac{mv^2}{r} = \frac{Ze^2}{r^2}$$

$$v^2 = \frac{Ze^2}{mr} \quad \rightarrow (i)$$

From Bohr's postulate we get

$$mvr = \frac{nh}{2\pi}, \quad v = \frac{nh}{2\pi mr}$$

$$v^2 = \frac{n^2 h^2}{4\pi^2 m^2 r^2} \quad \rightarrow (ii)$$

Equating eq. (i) and (ii)

$$\frac{Ze^2}{mr} = \frac{n^2 h^2}{4\pi^2 m^2 r^2}$$

$$r_n = \frac{n^2 h^2}{4\pi^2 m Ze^2}$$

r_n is the radius of the n^{th} orbit

$$r_H = 0.529 \times 10^{-8} \text{ cm} \\ = 0.529 \text{ \AA}$$

$$h = 6.62 \times 10^{-27} \text{ erg sec} \\ m = 9.10 \times 10^{-28} \text{ gm} \\ e = 4.8 \times 10^{-10} \text{ esu}$$

$$r_n = r_1 \times n^2 = 0.529 \times n^2 \text{ \AA}$$

The total energy

$$E = \text{P.E.} + \text{K.E.}$$

$$\text{K.E.} = \frac{1}{2} mv^2$$

$$\text{P.E.} = \int_{\infty}^r \frac{e^2}{r^2} dr = -\frac{e^2}{r}$$

$$\text{Thus the total energy } E = \frac{1}{2} mv^2 - \frac{e^2}{r} = \frac{1}{2} mv^2 - \frac{e^2}{r}$$

$$= \frac{e^2}{2r} - \frac{e^2}{r} = -\frac{e^2}{2r}$$

ϵ_0 = absolute permittivity of the medium. In vacuum $8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$