

possible values of n_r and k .
 for a particular value of n , the possible values of k are : 0, 1, 2, n while the corresponding values of n_r are $n, (n-1), (n-2), \dots, 0$.

But when $k=0$, b_n is 0 \rightarrow ellipse gets converted into straight line leading the moving electron to pass through the nucleus.

For $k=0$ is not acceptable

$$R = 1, 2, 3, \dots, n$$

$$n_r = (n-1), (n-2), (n-3), \dots, 0$$

$$\text{We have } \frac{b_n}{a_n} = \frac{k}{(k+n_r)}$$

when $n_r = 0$, b and a becomes the same.

Thus the ellipse gets reduced into a Bohr's circular orbit. Therefore, Bohr's circular orbit is only a special case in Sommerfeld's model

From Wave mechanics, the azimuthal quantum number is designated by l and l and k are related as

$$l = k - 1$$

Different Sommerfeld's Orbit

