

~~Legendre associated Laguerre polynomial~~

~~Legendre associated Laguerre polynomial~~

$R(r)$ or Ψ_r is a function of r , the radial distance from the nucleus. This is therefore called the radial part of the wave function or simply the radial function and abbreviated as R . It depends on the quantum numbers n and l .

Y_{θ} or $\Theta(\theta)$ is a function of θ

Y_{ϕ} or $\Phi(\phi)$ is a function of ϕ

$\Theta(\theta)$ and $\Phi(\phi)$ represent the angular part of the wave function. They may also be combined into a single function $Y_{\theta\phi}$. These functions depend primarily on the quantum numbers l and m_l .

Radial Wave function, R : The radial part of the wave function depends only on the values of ' n ' and ' l '. The radial function for the first three orbitals in the hydrogen-atom-like system

1s orbital ($n=1, l=0$) $R = 2 \left(\frac{Z}{a_0}\right)^{3/2} e^{-Zr/a_0}$

2s orbital ($n=2, l=0$) $R = \left(\frac{1}{2\sqrt{2}}\right) \left(\frac{Z}{a_0}\right)^{3/2} \left(2 - \frac{Zr}{a_0}\right) e^{-Zr/2a_0}$

2p orbital ($n=2, l=1$) $R = \frac{1}{2\sqrt{6}} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Zr}{a_0} e^{-Zr/2a_0}$

where Z is the nuclear charge, e the base of natural logarithms and a_0 is the radius of the first Bohr orbit. Its value is 52.9 pm is determined by $a_0 = \frac{h^2}{4\pi^2 m_e e^2}$